

# PROBLEMS AND SOLUTIONS

## EDITORS

*Curtis Cooper*  
CMJ Problems  
University of Central Missouri

*Jerzy Wojdylo*  
CMJ Problems, Elect  
Department of Mathematics  
Southeast Missouri State University  
One University Plaza  
Cape Girardeau, MO 63701  
cmjproblems@maa.org

*Charles N. Curtis*  
CMJ Solutions  
Mathematics Department  
Missouri Southern State University  
3950 Newman Road  
Joplin, MO 64801  
cmjsolutions@maa.org

This section contains problems intended to challenge students and teachers of college mathematics. We urge you to participate actively *both* by submitting solutions and by proposing problems that are new and interesting. To promote variety, the editors welcome problem proposals that span the entire undergraduate curriculum.

**Proposed problems** should be sent to **Jerzy Wojdylo**, either by email (preferred) as a pdf, TeX, or Word attachment or by mail to the address provided above. Whenever possible, a proposed problem should be accompanied by a solution, appropriate references, and any other material that would be helpful to the editors. Proposers should submit problems only if the proposed problem is not under consideration by another journal.

**Solutions to the problems in this issue** should be sent to **Chip Curtis**, either by email as a pdf, TeX, or Word attachment (preferred) or by mail to the address provided above, no later than June 15, 2017.

## PROBLEMS

**1111.** *Proposed by Greg Oman, University of Colorado, Colorado Springs, CO.*

Let  $\sum_{n=0}^{\infty} x_n$  be a real convergent series with positive terms. Prove that there is a subsequence  $\{x_{n_k}\}$  of  $\{x_n\}$  such that  $\sum_{k=0}^{\infty} x_{n_k}$  is irrational.

**1112.** *Proposed by Ovidiu Furdui, Technical University of Cluj-Napoca, Cluj-Napoca, Romania.*

Prove the following statements are equivalent for a real  $2 \times 2$  matrix  $A$ .

(a)  $\cosh A$  is singular.

(b)  $\cosh A = 0_2$  (the  $2 \times 2$  zero matrix).

(c)  $A = P \begin{pmatrix} 0 & \frac{(2m-1)\pi}{2} \\ \frac{-(2m-1)\pi}{2} & 0 \end{pmatrix} P^{-1}$  for some integer  $m$  and some real invertible matrix  $P$ .

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